Stability, Strategy-Proofness, and Cumulative Offer Mechanisms

Alexander WESTKAMP

(Universität Köln)

Abstract:

We consider the setting of many-to-one matching with contracts, where firms may demand multiple contracts but each worker desires at most one contract. We introduce three novel conditions - observable substitutability, observable size monotonicity, and nonmanipulatability - and show that when these conditions are satisfied, the cumulative offer mechanism is the unique mechanism that is stable and strategy-proof (for workers). Moreover, when the choice function of some firm fails any of our three conditions, one can construct unit-demand choice functions for the other firms such that no stable and strategyproof mechanism exists. In the final part of the paper, we characterize the class of choice functions for which the cumulative offer mechanism is guaranteed to yield a stable outcome.

Keywords: Matching with contracts, Stability, Strategy-proofness, Substitutability, Size monotonicity, Cumulative offer mechanism